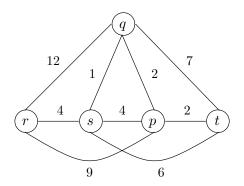
## Exam Distributed Algorithms

VU University Amsterdam, 18 December 2013, 12:00-14:45

(Answers can be given in English or Dutch. You may use the textbook Distributed Algorithms: An Intuitive Approach. Use of slides, handouts, laptop is not allowed.)

(The exercises in this exam sum up to 90 points; each student gets 10 points bonus.)

- 1. Suppose that Rana's algorithm is adapted as follows: Only quiet processes that have been quiet from some logical time < t (instead of  $\le t$ ) onward can take part in a wave tagged with time stamp t. Give an example of a finite computation for which termination would not be detected. (12 pts)
- 2. Show, using the technique to reduce garbage collection algorithms to termination detection algorithms, that indirect reference counting gives rise to Dijkstra-Scholten termination detection. (12 pts)
- 3. Run the Merlin-Segall algorithm on the following undirected weighted network, to compute all shortest paths toward process t. Give a computation that takes four rounds before the correct sink tree has been computed.



- 4. Argue that in the Gallager-Humblet-Spira algorithm, any fragment at a level  $\ell$  always contains at least  $2^{\ell}$  processes. (10 pts)
- 5. Apply the Itai-Rodeh ring size algorithm to an anonymous directed ring of size four. Give a computation in which all processes compute ring size three. (10 pts)
- 6. Suppose we adapt the Chandra-Toueg algorithm k-crash consensus for  $k < \frac{N}{2}$  as follows. If the coordinator  $p_c$  receives at least (instead of more than) k positive acknowledgments  $\mathbf{ack}$ , then  $p_c$  decides for its value. Give an example to show that this could lead to inconsistent decisions. (12 pts)
- 7. Let N=5 and k=1, and let the general g be Byzantine. Suppose that in pulse 1, g sends the value 1 to two lieutenants, and the value 0 to the other two lieutenants. Give a computation of  $Broadcast_g(5,1)$  (including a definition of the majority function) such that all lieutenants decide for 0. (12 pts)
- 8. Give an example of a computation of Dijkstra's token ring with N=K=4 that takes as long as possible before it reaches a correct configuration. (10 pts)