

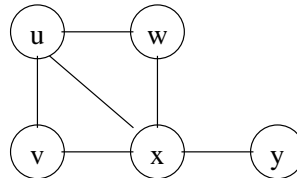
## Exam Distributed Algorithms

Free University Amsterdam, 26 May 2008, 8:45-11:30

*(At this exam, you may use copies of the slides without handwritten comments. Answers can be given in English or Dutch. Use of textbook, handouts, laptop is not allowed.)*

*(The exercises in this exam sum up to 90 points; each student gets 10 points bonus.)*

1. Give a transition system  $S$  and an assertion  $P$  such that  $P$  is a safety property but not an invariant of  $S$ . (5 pts)
2. Give a snapshot algorithm for undirected networks with non-FIFO channels, which uses (instead of piggybacking):
  - (1) marker messages  $\langle \mathbf{mkr}, n \rangle$ , where  $n$  is the number of basic messages sent into a channel before the marker message;
  - (2) acknowledgements; and
  - (3) temporary (local) freezing of the basic computation.(15 pts)
3. Consider the following network:



- Apply Cidon's algorithm to traverse this network with a depth-first search, starting at  $u$ . Give one possible traversal, together with all messages that are being communicated during this traversal. Let at least once a process receive the token from one process, while earlier it forwarded the token to another process. (10 pts)
4. Consider the Gallager-Humblet-Spira algorithm for computing a minimal spanning tree in a graph in which all edges have a unique weight. Suppose that in a fragment  $(L, FN)$ , a lowest-weight edge has just been reported at the core nodes, and at the same time a fragment  $(L', FN')$  with  $L' < L$  connects to this fragment (so subsumes level  $L$  and name  $FN$ ). How can we be sure that in the part  $(L', FN')$  there cannot be a lower-weight outgoing edge than the one just reported to the core nodes in  $(L, FN)$ ? (15 pts)

5. Apply the Itai-Rodeh ring size algorithm to a unidirectional ring of size 3 in the following two cases:
- (a) Suppose that all three processes initially choose the same identity. Show that the algorithm computes ring size 2. (6 pts)
  - (b) Suppose that only two processes initially choose the same identity. Show that the algorithm computes ring size 3. (9 pts)
6. Let  $N = 7$  and  $t = 2$ , and let the general  $g$  and one lieutenant be Byzantine. Give a scenario of  $Broadcast_g(7, 2)$  in which all correct lieutenants decide  $major(\{\perp, 0, 0, 1, 1, 1\})$ . (15 pts)
7. (a) Explain in detail why Fischer's mutual exclusion algorithm guarantees *mutual exclusion* and *no deadlock*. (9 pts)
- (b) Give an example to show that Fischer's mutual exclusion algorithm can give rise to *lockout*. (6 pts)