

**This is a “closed book” exam.**

No printed materials or electronic devices are admitted for use during the exam.

You are supposed to answer the questions **in English**.

*Wishing you lots of success with the exam!*

Points per question (maximum)

Q	1	2	3	4	5	6	7	8
	a b	a b	a b c	a b	a b c	a b		a b c
P	4 3	9 3	3 2 4	6 4	4 9 4	3 6	8	6 6 6

Total: 90

To pass the exam, it is sufficient to get at least 45 points.

## 1. The Synthetic Camera Model

- The Synthetic Camera Model is based on the working of an old-fashioned bellows camera. Describe how an image is constructed using the Synthetic Camera Model.
- One problem of a bellows camera (or the Synthetic Camera Model) is that it produces upside-down images. What 'trick' is used to correct for this problem, and why does this work?

## 2. Coordinate System Transformations

In OpenGL, the following coordinate systems are used (among others), here listed in alphabetical order:

- camera coordinates
  - clip coordinates
  - normalized device coordinates (NDC)
  - object coordinates
  - world coordinates
- Explain the role of each of these coordinate systems. By which mechanisms are coordinates transformed from one system to the other?
  - Which of these are homogeneous coordinates? Which ones are used by a vertex shader? Which ones by a fragment shader?

### 3. Texture Mapping

- a) Roughly speaking, texture mapping associates a discrete texel with each point on a geometric object. Name at least 3 problems that can occur with mapping textures, and explain each of the problems in reasonable detail.
- b) Mapping of 2-dimensional textures to non-flat 3-dimensional surfaces can be quite complex. Describe a two-step solution that can simplify the mapping.
- c) In a program, you are using the following fragment shader:

```
in varying vec2 tex_coords;
uniform sampler2D my_texture;

void main(){
    gl_FragColor = mix(texture(my_texture, tex_coords),
                        vec4(0.55,0.27,0.07,1.0), 0.3);
}
```

- i What does this fragment shader do?
- ii Supposed, you are confused by the way the texture is used and you wish to debug your program. Write a version of this fragment shader that displays a visual representation of the texture coordinates instead of the “true” colors.

### 4. Color

- a) Explain the RGBA color model, as used by OpenGL. How does the CMY model relate to RGB? Where are RGB and CMY used, predominantly?
- b) Write GLSL code (or similar syntax) for a simple fragment shader that implements a non-photorealistic, “comic style” effect of using only a limited number of colors. More precisely, your fragment shader shall allow  $n$  gradations of color intensity in each of the R,G,B channels. (Choose your own  $n$ .) The shader has the following parameters:  
in varying vec4 color;  
out varying vec4 gl\_FragColor;  
You can use the following GLSL function: `genType trunc (genType x)` that returns a value equal to the nearest integer to  $x$  whose absolute value is not larger than the absolute value of  $x$ .

## 5. Illumination

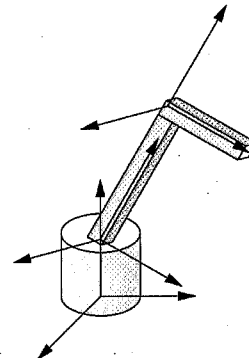
- Explain the difference between a *local* illumination model and a *global* illumination model, and give an example of each of these.
- Explain how specular reflection is computed in the Blinn-Phong lighting model. Which material properties are used in this model? Make a sketch of the involved vectors; which added vector was Blinn's contribution to Phong's model and what is its purpose?
- With OpenGL3, you can implement an illumination model either in the vertex shader or in the fragment shader. Explain the advantages of the two approaches, compared to each other.

## 6. Vertices and Fragments

- Explain the concepts *vertex*, *fragment*, *pixel*, related to each other.
- There are two units actually removing data from the rendering pipeline, clipping and hidden-surface removal. Where are they placed inside the rendering engine, and why? On which type of data do they operate?

## 7. Robot Components

The robot arm shown on the right can be moved in three ways, as shown in the diagram: The base can be rotated on the ground by an angle  $\alpha$ , the lower arm can be rotated by angle  $\beta$  relative to the base, and the upper arm can be rotated by angle  $\gamma$  relative to the lower arm.



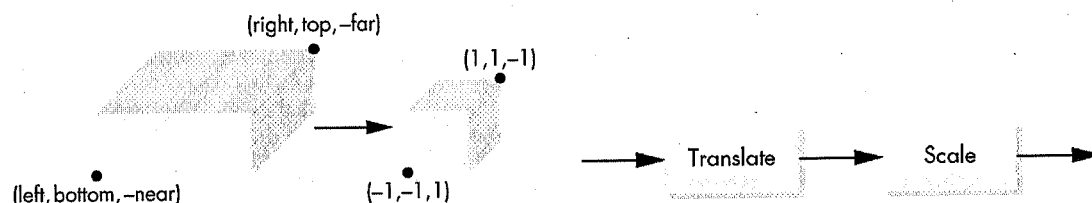
Write a method `void robot(float alpha, float beta, float gamma)` in Java (or in similar syntax) that draws the robot arm. You can assume there are three objects called `base`, `lower`, and `upper` with the following methods:

```
void render(Mat4 modelview) // renders this object based on the matrix
float get_height() // returns the height of the object
```

Hint: all you need to do is compute model-view matrices and call `render()` on the respective objects. You can assume to have a library of matrix operations like the one used in class.

## 8. Orthographic Projection

A call to `MatrixMath.ortho(left, right, bottom, top, near, far)` defines a viewing volume for orthogonal projection. `ortho` computes a matrix  $P$ :



As shown in the diagram (left), the effect of the matrix  $P$  is to map the viewing volume to the canonical volume. The right side of the diagram indicates that this mapping can be done in two steps, first a *translate* (moving the center of the viewing volume to the origin) and then a *scale*, bringing the volume to the size  $2 \times 2 \times 2$ .

**Hint:** To save work, simply abbreviate *left*, *right*, *bottom*, *top*, *near*, *far* by their first letters:  $L$ ,  $R$ ,  $B$ ,  $T$ ,  $N$ ,  $F$ .

- The translation step can be performed by using a translation matrix  $T(dx, dy, dz)$ . Compute  $dx, dy, dz$  and show that your  $T(dx, dy, dz)$  translates the points  $[L, B, -N, 1]^T$  and  $[R, T, -F, 1]^T$  to coordinates that lie symmetrically around the origin!
- The scaling step can be performed by using a matrix  $S(sx, sy, sz)$ . Compute  $sx, sy, sz$  and show that your  $S(sx, sy, sz)$  scales the translated corners of the viewing volume (the results from part a) to the respective corners of the canonical viewing volume, namely  $(-1, -1, 1)$  and  $(1, 1, -1)$ !
- Compute the overall matrix  $P$  from  $S(sx, sy, sz)$  and  $T(dx, dy, dz)$ ! Does it matter if you compute either  $P = S \cdot T$  or  $P = T \cdot S$ ? Explain why!