

Language disclaimer:

You are kindly asked to answer the questions using the English language. However, if it helps clarifying your answers, you may use *some* Dutch here and there. Doing so, *will not affect* your result.

Allowed material:

This is an “*open book*” exam. For answering the questions, you are allowed to use all kinds of written material like textbooks, printouts of the lecture slides, your own notes, etc. However, it is **not allowed** to use any electronic equipment or any means of communication.

Wishing you lots of success with the exam!

Points per question (Normering)

Q	1	2	3	4	5	6	7	8
	a b	a b c	a b c d	a b c d e	a b	a b	a b c	a b c
P	3 3	3 5 4	4 5 5 4	1 4 1 1 4	4 6	4 8	2 3 3	4 5 4

Total: 90 (+10 bonus) = 100

1. Human Visual System

- Explain the properties of the human visual system as far as they are relevant for the perception of images generated by computer graphics! Explain human color perception, the CIE standard observer curve, and lateral inhibition!
- What can a computer-graphics application do to work around the properties of the human visual system, namely standard observer curve and lateral inhibition?

2. Viewports

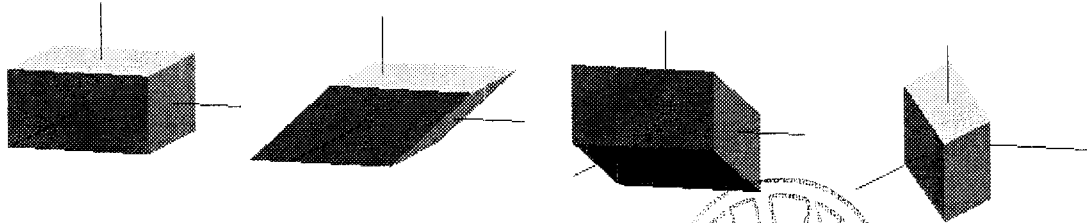
- Explain the terms *viewport* and *aspect ratio*! Give a formula that expresses the aspect ratio for a given viewport!
- Assume, an OpenGL application shall maintain the aspect ratio of its output a_v , even when a user resizes the window. In that case, the application shall use the maximal possible viewport that maintains a_v and that still fits into the reshaped window with its aspect ratio a_w . The viewport shall be centered in the window.

Given a_v and a_w , how many different cases have to be distinguished for finding such a maximal viewport? For each case, draw a simple sketch that shows the window, the viewport, and their respective width and height!

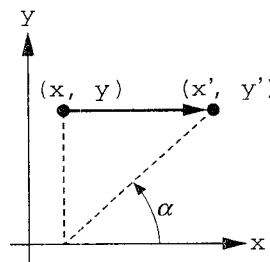
- c) Write a callback function in the C language using OpenGL (the GLUT library) that selects the viewport according to part b! Which (GLUT) function has to be used to register this callback?

3. Shear

The following pictures show (from left to right) a cube, and the same cube sheared along the X axis, the Y axis, and the Z axis.



- a) The following drawing shows how the shear along the X-axis can be represented depending on a shearing angle α . Make similar drawings, one for the shear along the Y axis (angle β), and one for the shear along the Z axis (angle γ), according to the above picture!

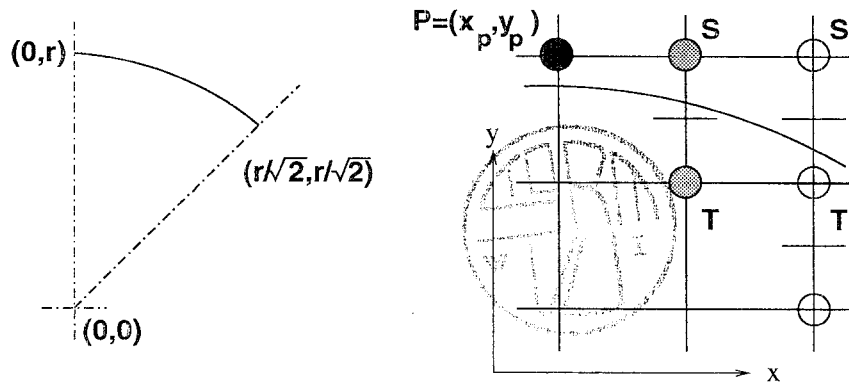


- b) Determine the shear matrices $H_x(\alpha)$, $H_y(\beta)$, and $H_z(\gamma)$, corresponding to part a!
- c) Implement a C function `void glShearX(GLfloat alpha)` that works like `glTranslate` or `glRotate` (affecting the currently active transformation matrix by multiplying $H_x(\alpha)$ to it! You can assume that a function `cot()` is available.
- d) Assume you have implemented the function `glShearX`, and also (analogously) `glShearY` and `glShearZ`. Determine a shear matrix $H(\alpha, \beta, \gamma)$ that combines the effects of $H_x(\alpha)$, $H_y(\beta)$, and $H_z(\gamma)$!

Is it possible to implement a function `glShearXYZ(alpha, beta, gamma)` by a combination of calls to `glShearX`, `glShearY`, and `glShearZ`? Explain why!

4. Bresenham's Algorithm

Mr. Bresenham also developed an algorithm for drawing circles. It works similar to his famous line drawing algorithm. The following picture shows at its left side the second octant of a circle with radius r and origin $(0, 0)$. In this octant, the arc that is part of the circle can be drawn, starting from the 12 o'clock position, by incrementing x and choosing the y coordinate closest to the circle. (Points (x, y) lie on the circle iff $x^2 + y^2 = r^2$)



For any point (x, y) , we can use the decision variable $d = x^2 + y^2 - r^2$.
 $d = 0$ if the point lies on the circle. $d > 0$ if the point lies outside, and $d < 0$ if the point lies inside the circle.

- Assume the last point that has been drawn is $P = (x_p, y_p)$ (see the picture above, on the right side). The next point for drawing the circle is chosen from S and T . Give the formula for d for the midpoint between S and T !
- Bresenham's algorithm works incrementally. The decision variable d' shall be used for choosing the next point, after one of S or T has been chosen. For both cases, give the respective formula for d' , relative to d !
- For starting at the 12 o'clock position, give the initial value for d !
- The algorithm works most efficiently, if only integer arithmetic can be used. Assume that all x and y coordinates, and the radius r are given as integer parameters. Give an initialization for an integer-valued decision variable d_i that closely approximates d !
- Implement a C function `void DrawArc(int Radius)` that draws the second octant of a circle with the center at the origin $(0, 0)$ (as shown in the above picture)! Assume, you have a function `void setPixel(int x, int y)` available. Your function shall not use any floating point arithmetic.

5. Morphing

Transformation of object shapes from one form to another is called morphing. For morphing, object shapes are defined by so-called *key frames* between which several interpolative steps are generated for a smooth morphing transition. Suppose, you have a complex graphical object represented by the following, recursive C data structure.

```
typedef struct position {
    /* relative to the parent node in the tree: */
    GLfloat tx, ty, tz; /* translation */
    GLfloat sx, sy, sz; /* scaling */
    GLfloat rx, ry, rz; /* rotation axis */
    GLfloat angle; /* angle of rotation */
} position;
```

```

typedef struct node {
    struct position *p1,*p2;    /* key frames 1 and 2    */
    void (*attrib_function)(); /* setting attributes,  */
                                /* if not NULL          */
    void (*drawing_function)(); /* drawing the object    */
    struct node *sibling;      /* list of sibling nodes */
    struct node *child;        /* list child nodes      */
} node;

```

a) Implement a C function:

```

void interpolate(struct position *p1, struct position *p2,
                 struct position *p3, GLfloat percentage)

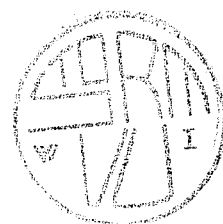
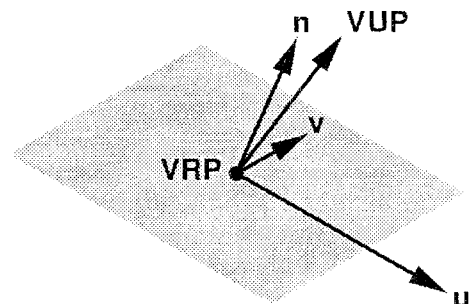
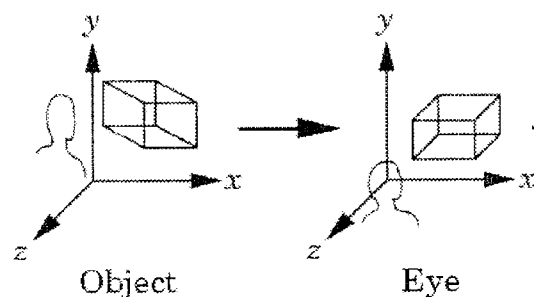
```

that computes in p3 the interpolation between p1 and p2 for a position of percentage!
The valid range for percentage is 0..1, where 0 corresponds to p1 and 1 corresponds to p2.

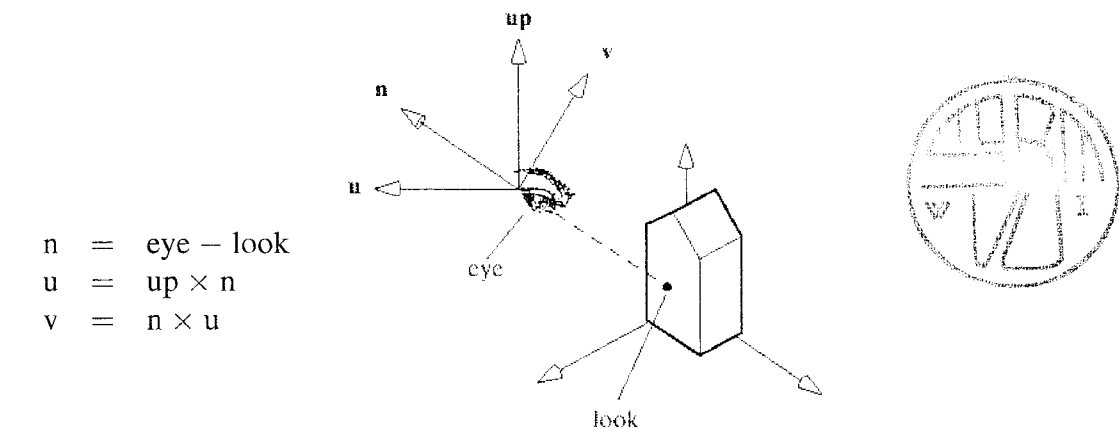
b) Using your function `interpolate()`, now implement a C function (based on OpenGL) `void morph(struct node *tree, GLfloat percentage)`, that displays the graphical object given in tree! Your function shall produce a single image of the object that corresponds to a frame that lies percentage % between p1 and p2. (Your function has to traverse all nodes of the tree data structure.) The function `attrib_function` allows to set attributes like color or material properties; it shall only be called if the pointer is not NULL.

6. Viewing

a) Explain (briefly) how the transformation from object (world) coordinates to eye (camera) coordinates contributes to a viewing API! What are the components of a u-v-n viewing coordinate system?



- b) The function `gluLookAt (eyex, eyey, eyez, lookx, looky, lookz, upx, upy, upz)` internally uses a u-v-n coordinate system:



`gluLookAt` normalizes n, u, v to unit length and uses the normalized vectors to build up the viewing matrix:

$$V = \begin{pmatrix} u_x & u_y & u_z & d_x \\ v_x & v_y & v_z & d_y \\ n_x & n_y & n_z & d_z \\ 0 & 0 & 0 & 1 \end{pmatrix} \quad (d_x, d_y, d_z) = (-\text{eye} \cdot u, -\text{eye} \cdot v, -\text{eye} \cdot n)$$

Show that u, v, n are mutually perpendicular (orthogonal)!

Show that the matrix V properly converts object coordinates to eye coordinates by demonstrating that it maps *eye* to the origin $(0, 0, 0, 1)^T$, u to $(1, 0, 0, 0)^T$, v to $(0, 1, 0, 0)^T$, and n to $(0, 0, 1, 0)^T$!

7. Polygon Shading

- Explain the basic idea of the Phong reflection model! Draw a simple figure that shows the vectors involved in computing the shade of a given point on the surface of an object!
- Explain how *flat shading* works, for example for a polygonal mesh! What are the advantage and the disadvantage of flat shading?
- Explain *Phong shading* and how it improves over the disadvantage of flat shading!

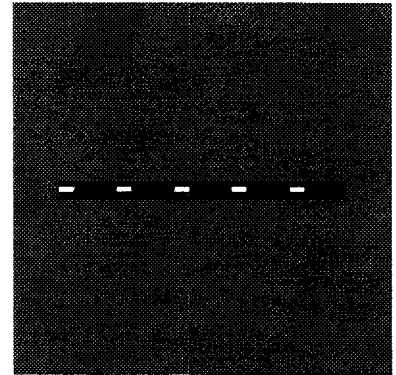
8. Texture

Write a program that shows a road: The road is 15 meters long and 1 meter wide. Every 3 meters, there is a white dash painted on the asphalt. Each dash is 75 cm long and 25 cm wide. The pattern of the road shall be determined by an 8×8 texture pattern that is mapped onto a quad. Start with the following main program. The desired output of your program is shown on the right side.

```

int main (int argc, char** argv)
{
    glutInit(&argc, argv);
    glutInitDisplayMode(GLUT_RGB | GLUT_SINGLE );
    glutInitWindowSize (500, 500);
    glutCreateWindow (argv[0]);
    glClearColor(0.0,0.0,0.7,1.0);
    glMatrixMode(GL_PROJECTION);
    glLoadIdentity();
    gluOrtho2D(-10.0,10.0,-10.0,10.0);
    glMatrixMode(GL_MODELVIEW);
    glLoadIdentity();
    Init_Texture();
    glutDisplayFunc(Display);
    glutMainLoop();
    return 0;
}

```



- a) Define and initialize the data structure for your 8×8 texture!
- b) Implement the function `void Init_Texture(void)` that does all initialization necessary for the texturing!
- c) Implement the function `void Display(void)` that actually displays the road!

