Neural Networks

8 June 1998

Grading: In total you can get 100 points. You get 10 points free. Grade = number of points/10.

Problem A (30 points) Perceptron

- 1 (5 p) Describe the perceptron training algorithm. Formulate the update rule for a single-layer perceptron.
- 2 (5 p) Describe the pocket algorithm (any variant of it).
- 3 (5 p) Define the concept of linear separability.
- **4** (**5 p**) Compare both algorithms (perceptron and pocket) with respect to the following criteria: convergence, speed, robustness (by 'robustness' we mean here the following property: the longer the network is trained the better accuracy is achieved).
- 5 (3 p) Let us consider two sets of points in R²:

$$A = \{(x,y) \mid x^2 + y^2 < 144, x, y \text{ are integer}\}$$

and

$$B=\{(x,y) \mid x^2+y^2>144, x, y \text{ are integer}\}.$$

Are these two sets lineary separable? Justify your answer.



6 (7 p) Let us consider similar sets of sets of points in \mathbb{R}^4 :

A={
$$(x,y, z, t) | x^2+y^2<144, z=x^2, t=y^2, x, y, z, t \text{ are integer}}$$

and

B={
$$(x,y, z, t) | x^2+y^2>144, z=x^2, t=y^2, x, y, z, t are integer}$$
.

Are these two sets lineary separable? Justify your answer.

Problem B (25 points) Backpropagation

Let us consider a feed-forward network shown in figure 1. Here we assume that the hidden units have no bias and that the activation function is given by $S(net)=net^3$. (Let us recall that $(x^3)'=3x^2$).

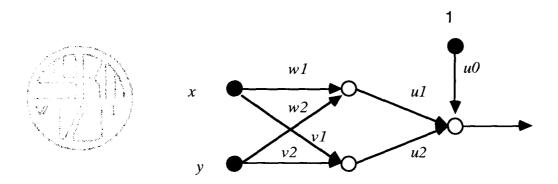


Figure 1. A 2:2:1 feed-forward network with 7 weights.

- a) (5 p) Express the output of this network as a function of nine variables: x, y, w_1 , w_2 , v_1 , v_2 , u_0 , u_1 , u_2 (write a formula).
- **b)** (10 p) Formulate update rules for weights u_0 , u_1 and w_1 . You don't have to derive these rules—just apply the generalized delta rule used in the backpropagation algorithm.
- c) (5 p) Can this network be trained to solve the XOR problem? Briefly justify your answer.
- **d)** (**5 p)** Let us suppose that the training parameter is set to a negative value (e.g. -0.5). How would it affect the training process? Would it converge? Would the result be a local minimum?

Problem C (15 points) Constructive Algorithms

- a) (10 p.) Describe in detail one (and only one) of the following 2 algorithms:
 - the upstart algorithm
 - the cascade correlation algorithm
- **b)** (5 **p.**) Which of these two algorithms is not suitable for function approximation? Justify your answer.

Problem D (20 points) Overview

Let us consider the following 5 types of networks:

- a) winner-take-all networks (WTA networks)
- b) feed-forward networks (BP networks)
- c) Radial Basis Function networks (RBF networks)
- d) Self-organizing maps (Kohonen networks)
- e) Hopfield networks

Characterize each of these networks with respect to the following aspects:

- 1) types of problems that can be solved with these networks: classification, function approximation, data clustering,
- 2) type of learning algorithm: supervised/unsupervised/mixed,
- 3) speed of training,
- 4) the amount of training parameters (list them).

For each network give an example of its application.