vrije Universiteit amsterdam

Faculty of Economics and Business Administration

Exam:	Investments 3.4
Code:	E_EBE3_INV
Coordinator:	dr. D. Stefanova
Date:	March 26, 2012
Time:	15.15
Duration:	2 hours and 45 minutes
Calculator allowed:	Yes
Graphical calculator allowed:	Yes
Number of questions:	20 multiple choice questions and 4 open questions
Type of questions:	Open/ multiple choice
Answer in:	English

Remarks: Be concise and complete in your answers (including calculations). Always explain your answers, even if not explicitly called for. Use your time efficiently, using the maximum number of points per question as a guideline.

Credit score:	The maximum possible scores for each part and question are indicated. In total, you can earn 100 points. Your final exam grade is determined by dividing the number of points by 10.
Grades:	The grades will be made public on: April 8 2010.
Inspection:	Thursday, April 11 2010 at 10.00 in room 2A-33.
Number of pages:	12 (including front page)

Good luck!

PART 1 (MULTIPLE CHOICE; 40 points at maximum)

Read the questions and answers carefully and write down your answer on your answer sheet. Your final score is determined as (# correct answers - 2) * 40/18. Negative scores for this part of the exam are set to zero.

1. An investor invests 30 percent of his wealth in a risky asset with an expected rate of return of 0.15 and a variance of 0.04 and 70 percent in a T-bill that pays 6 percent. His portfolio's expected return and standard deviation are _____ and _____, respectively.
A. 0.114; 0.12
B. 0.087; 0.06
C. 0.295; 0.12
D. 0.087; 0.12
E. 0.795; 0.14

2. Consider an investment opportunity set formed with two securities that are perfectly negatively correlated. The global minimum variance portfolio has a standard deviation that is always
A. greater than zero.
B. equal to zero.
C. equal to the sum of the securities' standard deviations.
D. equal to -1.
E. between zero and -1.

3. In the single-index model represented by the equation $r_i = E(r_i) + \beta_i F + e_i$, the term e_i represents
A. the impact of unanticipated macroeconomic events on security i's return.
B. the impact of unanticipated firm-specific events on security i's return.
C. the impact of anticipated macroeconomic events on security i's return.
D. the impact of anticipated firm-specific events on security i's return.
E. the impact of changes in the market on security i's return.

4. According to the Capital Asset Pricing Model (CAPM),
A. a security with a positive alpha is considered overpriced.
B. a security with a zero alpha is considered to be a good buy.
C. a security with a negative alpha is considered to be a good buy.
D. a security with a positive alpha is considered to be underpriced.
E. a security with a positive beta is considered to be underpriced.

5. A security has an expected rate of return of 0.10 and a beta of 1.1. The market expected rate of return is 0.08 and the risk-free rate is 0.05. The alpha of the stock is
A. 1.7%.
B. -1.7%.
C. 8.3%.
D. 5.5%.
E. -5.5%.

6. Consider the multifactor model APT with two factors. Portfolio A has a beta of 0.75 on factor 1 and a beta of 1.25 on factor 2. The risk premiums on the factor 1 and factor 2 portfolios are 1% and 7%, respectively. The risk-free rate of return is 7%. The expected return on portfolio A is _____ if no arbitrage opportunities exist.
A. 13.5%
B. 15.0%
C. 16.5%
D. 23.0%
E. 18.7%

7. In an efficient market the correlation coefficient between stock returns for two non-overlapping time periods should be
A. positive and large.
B. positive and small.
C. zero.
D. negative and small.
E. negative and large.

8. Each of two stocks, C and D, are expected to pay a dividend of $3 in the upcoming year. The expected growth rate of dividends is 9% for both stocks. You require a rate of return of 10% on stock C and a return of 13% on stock D. The intrinsic value of stock C ____.
A. will be greater than the intrinsic value of stock D
B. will be the same as the intrinsic value of stock D
C. will be less than the intrinsic value of stock D
D. cannot be calculated without knowing the market rate of return
E. None of these is correct.

9. Suppose two portfolios have the same average return, the same standard deviation of returns, but Aggie Fund has a higher beta than Raider Fund. According to the Sharpe measure, the performance of Aggie Fund

A. is better than the performance of Raider Fund.
B. is the same as the performance of Raider Fund.
C. is poorer than the performance of Raider Fund.
D. cannot be measured as there is no data on the alpha of the portfolio.
E. None of these is correct.

10. You want to evaluate three mutual funds using the Treynor measure for performance evaluation. The risk-free return during the sample period is 6%. The average returns, standard deviations, and betas for the three funds are given below, in addition to information regarding the S&P 500 index.

	Average Return	Standard. Deviation	Beta
Fund A	13%	10%	0.5
Fund B	19%	20%	1.0
Fund C	25%	30%	1.5
S&P 500	18%	16%	1.0

The fund with the highest Treynor measure is _____.

A. Fund A
B. Fund B
C. Fund C
D. Funds A and B are tied for highest
E. Funds A and C are tied for highest

11. A Treasury bond due in one year has a yield of 6.2%; a Treasury bond due in 5 years has a yield of 6.7%. A bond issued by Xerox due in 5 years has a yield of 7.9%; a bond issued by Exxon due in one year has a yield of 7.2%. The default risk premiums on the bonds issued by Exxon and Xerox, respectively, are

A. 1.0% and 1.2%
B. 0.5% and .7%
C. 1.2% and 1.0%
D. 0.7% and 0.5%
E. None of these is correct.

12. Consider two bonds, A and B. Both bonds presently are selling at their par value of $1,000. Each pays interest of $120 annually. Bond A will mature in 5 years while bond B will mature in 6 years. If the yields to maturity on the two bonds change from 12% to 10%, _____.
A. both bonds will increase in value, but bond A will increase more than bond B
B. both bonds will increase in value, but bond B will increase more than bond A
C. both bonds will decrease in value, but bond A will decrease more than bond B
D. both bonds will decrease in value, but bond B will decrease more than bond A
E. None of these is correct.

13. The pure yield curve can be estimated
A. by using zero-coupon Treasuries.
B. by using stripped Treasuries if each coupon is treated as a separate "zero."
C. by using corporate bonds with different risk ratings.
D. by estimating liquidity premiums for different maturities.
E. by using zero-coupon Treasuries and by using stripped Treasuries if each coupon is treated as a separate "zero."

14. Given the time to maturity, the duration of a zero-coupon bond is higher when the discount rate is
A. higher.
B. lower.
C. equal to the risk free rate.
D. The bond's duration is independent of the discount rate.
E. None of these is correct.

15. Immunization is not a strictly passive strategy because
A. it requires choosing an asset portfolio that matches an index.
B. there is likely to be a gap between the values of assets and liabilities in most portfolios.
C. it requires frequent rebalancing as maturities and interest rates change.
D. durations of assets and liabilities fall at the same rate.
E. None of these is correct.

16. The current market price of a share of AT&T stock is $50. If a call option on this stock has a strike price of $45, the call
A. is out of the money.
B. is in the money.
C. sells for a higher price than if the market price of AT&T stock is $40.
D. is out of the money and sells for a higher price than if the market price of AT&T stock is $40.
E. is in the money and sells for a higher price than if the market price of AT&T stock is $40.

17. A covered call position is
A. the simultaneous purchase of the call and the underlying asset.
B. the purchase of a share of stock with a simultaneous sale of a put on that stock.
C. the short sale of a share of stock with a simultaneous sale of a call on that stock.
D. the purchase of a share of stock with a simultaneous sale of a call on that stock.
E. the simultaneous purchase of a call and sale of a put on the same stock.

18. Which of the following factors affect the price of a stock option
A. the risk-free rate.
B. the riskiness of the stock.
C. the time to expiration.
D. the expected rate of return on the stock.
E. the risk-free rate, the riskiness of the stock, and the time to expiration.

19. Which of the inputs in the Black-Scholes Option Pricing Model are directly observable
A. the price of the underlying security.
B. the risk free rate of interest.
C. the time to expiration.
D. the variance of returns of the underlying asset return.
E. the price of the underlying security, the risk free rate of interest, and the time to expiration.

20. A hedge ratio of 0.70 implies that a hedged portfolio should consist of
A. long 0.70 calls for each short stock.
B. short 0.70 calls for each long stock.
C. long 0.70 shares for each short call.
D. long 0.70 shares for each long call.
E. None of these is correct.

PART 2 (OPEN QUESTIONS; 60 points at maximum)

QUESTION 1. (15 points) Equilibrium pricing models

Part a. (3 points)
Give the formula of the CAPM and explain its notation. What are the assumptions underlying the CAPM? How do they relate to empirical evidence?

Part b. (2 points)
Consider the multifactor APT with two factors. The risk premiums on the factor 1 and factor 2 portfolios are 5% and 6%, respectively. Stock A has a beta of 1.2 on factor 1, and a beta of 0.7 on factor 2. The expected return on stock A is 17%.

If no arbitrage opportunities exist, what should the risk-free rate of return be?

Part c. (3 points)
Security A has a beta of 1.0 and an expected return of 12%.
Security B has a beta of 0.75 and an expected return of 11%.
The risk-free rate is 6%.

Explain the arbitrage opportunity that exists; explain how an investor can take advantage of it. Give specific details about how to form the portfolio, what to buy and what to sell (*Hint: form a portfolio of security A and the risk-free asset*).

Part d. (3 points)
Consider the regression equation:

$$r_i - r_f = g_0 + g_1 b_i + g_2 s^2(ei) + e_{it}$$

where: $r_i - r_t$= the average difference between the monthly return on stock **i** and the monthly risk-free rate, b_i= the beta of stock **I,** $s^2(ei)$ = a measure of the nonsystematic variance of the stock **i.**
If you estimated this regression equation and the CAPM was valid, what would you expect the estimated coefficients g_0, g_1, and g_3 to be? Why?

Part e. (4 points)
Consider the Fama-French 3-factor model:

$$r_i = \alpha_i + \beta_i r_M + \gamma_i SMB + \delta_i HML + e_i$$

where r_i is the return of a stock i, r_M is the market return, SMB is a factor that proxies for size, and HML – for value. The variances of the three factors are respectively σ^2_M, σ^2_{SMB} and σ^2_{HML}. The variance of the idiosyncratic source of risk is $\sigma^2(e)$ and it is the same for all stocks i.

Assume that the idiosyncratic sources of risk are uncorrelated, and that the three factors are uncorrelated as well.

i. Give an expression for the systematic risk of stock i in terms of the variances of the three factors.
ii. Construct an equally weighted portfolio of 10 stocks. What is its non-systematic risk component? Compare it to the non-systematic risk component of the individual stocks.
iii. Consider three stocks, i={1,2,3}. Construct a portfolio out of the three stocks that has zero exposure to the size factor, and an exposure of 1 to the value factor. Provide the system of equations to be used to solve for the weights. You do not need to find the explicit solution for the weights.

QUESTION 2. (15 points) Portfolio construction and performance measurement

Part a. (6 points)

Consider two risky assets, A and B. Denote by r_A the return of risky asset A, and r_B the return of risky asset B. Their respective standard deviations are σ_A ans σ_B. The two assets are correlated and their correlation coefficient is given by ρ.
Further, consider a portfolio P of the two assets, with weights ω and (1-ω) respectively.

i. Give an analytic expression of the return of the portfolio (r_P) and its variance (σ_P^2). What is the expected return of the portfolio $E[r_P]$?

ii. If the correlation between the two assets is ρ= -1, solve for the weights of a perfectly hedged portfolio.

iii. Consider an investor who has the following utility function:

$$U = E[r_P] - \frac{1}{2} A \sigma_P^2$$

where A is the level of risk aversion of the investor. As well, the risk-free return is given by r_f .
Which value of A makes the investor indifferent between investing in the risky portfolio P and the risk-free asset? Give an analytic expression.

Part b. (6 points)

The following data are available relating to the performance of Monarch Stock Fund and the market portfolio:

	Monarch	Market Portfolio
Average Return	16%	12%
Standard Deviation of Returns	26%	22%
Beta	1.15	1.00
Residual Standard Deviation	1%	0%

The risk-free return during the sample period was 4%.

i. Calculate Sharpe's measure of performance for Monarch Stock Fund.
ii. Calculate Jensen's measure of performance for Monarch Stock Fund.
iii. What is the information ratio measure of performance evaluation for Monarch Stock Fund?
iv. If you wanted to evaluate the Seminole Fund using the M^2 measure, what percent of the adjusted portfolio would need to be invested in T-Bills? Calculate the M^2 measure.

Part c. (3 points)

You are evaluating the market timing ability of a portfolio manager. In order to do so, you use the following regression equation:

$$r_P - r_f = a + b\left(r_M - r_f\right) + c\left(r_M - r_f\right)^2 + e_P$$

where r_P is the return of the portfolio, r_f is the risk-free rate, r_M is the market return, and e_P is the error term.

i. How would you test for the timing ability of the portfolio manager, using the above regression equation? Give also a graphic interpretation.
ii. How would you define an ideal situation of perfect foresight (also give a graphic interpretation)? Using this, how could you compute the value of market timing?

QUESTION 3. (15 points) Fixed Income

Part a. (4 points)

You are given the following three coupon bonds with annual coupon payments.

Bond	Maturity	Coupon	Price	Yield to maturity	Notional
A	2	2%	$ 100.9897	1.4940 %	$ 100
B	2	6%	$ 108.8366	1.4831 %	$ 100
C	3	4%	$ 106.7183	1.6847 %	$ 100

Compute the zero rates z_1, z_2, z_3 (up to two decimal places) for maturities of 1, 2, and 3 years.

Part b. (6 points)

Using the data on the three coupon bonds in Part (a):

i. Compute the modified duration of the three bonds.
ii. Construct a portfolio that consists of a long position in 10 type A bonds, a short position in 30 type B bonds and a long position in 50 type C bonds. Obtain the value of the portfolio and the weights of each bond.
iii. Compute the modified duration of this portfolio.
iv. If you expect an upward shift in the term structure (i.e. an increase of all interest rates) by 200 basis points, what would be the percentage change in the value of the portfolio, based on duration approximation? If alternatively you expect a decrease by 50 basis points, what would be the percentage change in the value of the portfolio? Comment on the quality of the approximation in both cases.

Part c. (2 points)

The zero rates for maturities of 1, 2, and 3 years are given by z_1, z_2, and z_3. Obtain (analytically) the corresponding one-year forward rates for t=1, 2, 3 (f_1, f_2, f_3) in terms of the zero rates. Express the price of a 3-year coupon bond with annual coupon payments of C and face value of 100 using the forward rates.

Part d. (3 points)

Assume that you have a portfolio with duration of 1.8 and convexity of 6. The current yield curve is flat at 5%. Construct a new portfolio of zero coupon bonds with maturities of 2 and 5 years, and cash, such that it matches the duration and convexity of your portfolio.

QUESTION 4. (15 points) Option pricing

Part a. (3 points)

Discuss the differences in writing covered and naked calls (a naked call refers to writing a call on a stock that the investor does not own). Are risks involved in the two strategies similar or different? Explain.

Part b. (2 points)

An American-style call option with six months to maturity has a strike price of $35. The underlying stock now sells for $43. The call premium is $12.

i. Calculate the intrinsic value of the call
ii. What is the time value of the call?

Part c. (8 points)

Consider the following binomial tree for the evolution of the €/$ exchange rate over the period of 1 year, assuming 2 steps (t=0, t=1, t=2). The current exchange rate at t=0 is S_0 = 0.70 €/$. The annual interest rate is 3%, and the exchange rate can increase by 10% or decrease by 5% each period.

i. Draw the binomial price tree for (t=0, t=1, t=2).
ii. Calculate the risk-neutral probability of an upward movement and that of a downward movement.
iii. Consider a Dutch company that will have to pay $ 1 million in 1 year. The spot exchange rate today is S_0 = 0.70 €/$. The company wants to hedge itself against an unfavourable foreign exchange rate in 1 year, but would also like to gain from a depreciation of the US dollar. It has the following two options:
    A. Buy a standard call option with a strike price of X = 0.70 €/$ and expiry in one year;
    B. Buy a down-and-out barrier call option. This option behaves like a standard call option, except that it is terminated and becomes worthless once the

foreign exchange rate at any moment during the life of the option becomes equal or lower than the chosen barrier. It has a strike price of X = 0.70 €/$ and it is terminated if the exchange rate becomes equal to or falls below a barrier of 0.68 €/$.

Compute the price of the call option in (A) and of the barrier down-and-out call option in (B) using binomial pricing with 2 steps (t=0, t=1, t=2) and the binomial tree from (i).

Is there a difference in the prices of the standard call option and the down-and-out barrier call? Which one would you recommend to the company?

Part d. (2 points)

Replicate the pay-off structure below (known as 'short iron condor') using call or put options. On the horizontal axis you have the price of the underlying stock, and on the vertical axis – the pay-off at maturity.

NB. Mind the scale on the horizontal and the vertical axis.