

## Exam Distributed Algorithms

Vrije Universiteit Amsterdam, 31 May 2023, 18:45-21:30

*(You may use the textbook Distributed Algorithms: An Intuitive Approach. Use of slides, solutions to exercises, notes, laptop, calculator is not allowed.)*

*(The exercises in this exam sum up to 90 points; each student gets 10 points bonus.)*

1. Let the Dijkstra-Scholten algorithm be employed to detect termination of some centralized basic algorithm. Give an execution of the basic algorithm in which an active process  $q$  has a parent  $p$  in the Dijkstra-Scholten tree while  $q$  was made active for the last time by a process  $r \neq p$ . (10 pts)
  
2. Consider the weight-throwing termination detection algorithm with the counter  $credit_p$  for recording weight, to avoid underflow. Why does an active process that receives a basic message not return this weight to the initiator immediately, but only after it has become passive? (10 pts)
  
3. Consider Franklin's election algorithm for undirected rings (with non-FIFO channels).
  - (a) Give an example to show that an active process in election round  $n$  can receive a message for round  $n + 1$  before receiving the message for round  $n$  from this same direction, where these two messages carry different IDs. (8 pts)
  - (b) Argue that it cannot receive a message for two rounds ahead. (12 pts)

4. Consider the Bracha-Toueg  $k$ -crash consensus algorithm, with  $k < \frac{N}{2}$ . Let more than  $\frac{N+k}{2}$  processes choose the value  $b$  in the initial configuration. Argue that the correct processes will inevitably decide for  $b$  within three rounds. (10 pts)
  
5. Consider the heights  $(h_1, h_2)$  in the Walter-Welch-Vaidya mutual exclusion algorithm.
  - (a) Argue that the minimum  $h_1$ -value in the network never decreases during computations. (8 pts)
  - (b) Give an example where the minimum  $h_2$ -value in the network increases during a computation. (6 pts)
  
6. Suppose that in step 2 of the Kerberos authentication protocol, the authentication server would include the server ID  $S$  in the ticket it sends to the client. Explain how this would seriously hamper the applicability of the Kerberos protocol. (10 pts)
  
  
7.
  - (a) Consider the Winternitz signature scheme with  $k = 10$  and  $\ell = 3$ . Let 0100111010 be the hash of Alice's message to Bob. Explain how Alice signs her message, taking into account the checksum, and how Bob verifies this signature. (8 pts)
  - (b) Suppose the Winternitz signature from (a) is placed in the third leaf of a binary Merkle tree of depth 4 and used by Alice in a Merkle signature of a message to Bob. Explain concretely what the signature looks like and how this signature is employed by Bob to verify whether the public key is genuine. (8 pts)